

## New functionalities of Versions 3.1 and 3.2 of TFEL/MFront

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**Abstract** — MFront is a tool which allows easy implementation of arbitrary complex mechanical behaviours in an efficient way. Those implementations are portable between various finite element solvers and solvers based on FFT. MFront is part of the open-source TFEL project. The purpose of this paper is to highlight a selected set of features introduced in Versions 3.1 and 3.2 of TFEL.

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## 1 Overview of TFEL, MFront and MTest

The TFEL project is an open-source collaborative development of the French Alternative Energies and Atomic Energy Commission (CEA) and Électricité de France (EDF) in the framework of the PLEIADES platform (1). TFEL provides mathematical libraries which are the basis of the MFront code generator and the MTest solver (2, 3).

MFront translates a set of closely related domain specific languages into plain C++ on top of the TFEL library. Those languages are meant to be easy to use and learn by researchers and engineers and cover three kinds of material knowledge: material properties (Young modulus, thermal conductivity, etc.), mechanical behaviours<sup>1</sup> and simple point-wise models (such as material swelling

<sup>1</sup>Among the many projects aiming at easing the implementation of mechanical behaviours (see for example (4–6)), MFront can be compared to the ZebFront code generator which is part of ZMat library (7). A comprehensive

used in fuel performance codes).

Authors of `MFront` paid particular attention to the robustness, reliability and numerical efficiency of the generated code, in particular for mechanical behaviours: various benchmarks show that `MFront` implementations are competitive with native implementations available in the `Cast3M` (9), `Code_Aster` (10), `Europlexus` (11), `Abaqus/Standard`, `Abaqus/Explicit` (12, 13), `Cyrano3` (14) and `Galileo` solvers.

Portability is also a very important issue: a behaviour written in `MFront` shall be usable in any solver for which an interface exists. In addition to the aforementioned solvers, interfaces exist for: `Ansys` (15), `ZMat` (7), `CalculiX` (16, 17). This paper will also describe the generic interface and the `MFrontGenericInterfaceSupport` project which allow developers of home-brew solvers to add support for external behaviours in their code.

## 2 Some improvements of the `TFEL/Material` library

The `TFEL/Material` provides functions to handle advanced yield criteria, such as:

- The Hosford 1978 yield criterion (18), which is defined as follows:

$$\sigma_{\text{eq}}^H = \sqrt{\frac{1}{2} (|\sigma_1 - \sigma_2|^a + |\sigma_1 - \sigma_3|^a + |\sigma_2 - \sigma_3|^a)}$$

where  $\sigma_1$ ,  $\sigma_2$  and  $\sigma_3$  are the eigenvalues of the stress<sup>2</sup>.

- The Barlat 2004 yield criterion (19), defined as follows:

$$\sigma_{\text{eq}}^B = \sqrt{\frac{1}{4} \left( \sum_{i=0}^3 \sum_{j=0}^3 |s'_i - s''_j|^a \right)} \quad \text{with} \quad \begin{cases} \underline{s}' = \underline{\mathbf{L}}' : \underline{\sigma} \\ \underline{s}'' = \underline{\mathbf{L}}'' : \underline{\sigma} \end{cases}$$

where  $s'_i$  and  $s''_i$  are the eigenvalues of two transformed stresses  $\underline{s}'$  and  $\underline{s}''$ . The linear transformations  $\underline{\mathbf{L}}'$  and  $\underline{\mathbf{L}}''$  describe the orthotropy of the yield surface.

Those two yield criteria are based on the eigenvalues of the stress.<sup>3</sup> The computation of the second derivative, required to build the jacobian of the implicit system, is thus quite involved. The implementations of those two criteria closely follows the work of Scherzinger (21)<sup>4</sup>.

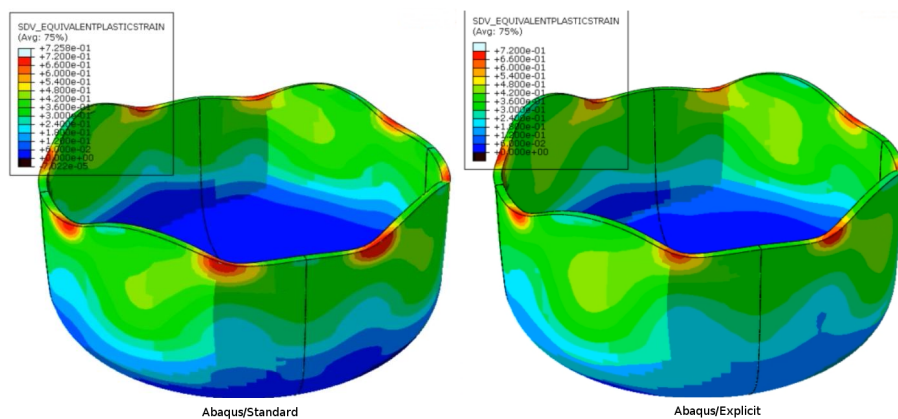


Figure 1: Simulation of the deep drawing of a highly anisotropic 2090-T3 aluminum alloy sheet comparison between these two solutions has been presented at the ZSet User Days (8).

<sup>2</sup>When  $a$  goes to infinity, the Hosford stress reduces to the Tresca stress criterion. When  $n = 2$  the Hosford stress reduces to the von Mises stress criterion.

<sup>3</sup>When  $a$  is an integer, Soare and Barlat (20) proposed another approach, not yet implemented in `TFEL`.

<sup>4</sup>In particular, special care has been taken to avoid overflow in the evaluation of those criteria.

Figure 1 shows an application of this development to the simulation of the deep drawing of a highly anisotropic 2090-T3 aluminum alloy sheet as discussed by Yoon et al. (22). This figure shows that the results obtained by `Abaqus/Standard` and `Abaqus/Explicit` are close, illustrating the portability of the implementation from one solver to another.

### 3 Mechanical behaviours

#### 3.1 Bricks

Bricks are a new feature introduced in Version 3.0. A brick is meant to simplify the implementation of a certain class of behaviours and hide tedious details for the user to focus on the physics. The following bricks are available:

- the `StandardElasticity` brick (Version 3.0), described in a previous paper (23).
- the `DDIF2` brick (Version 3.1), which describes a damage behaviour used in fuel performance codes (24).
- the `FiniteStrainSingleCrystal` brick (Version 3.0), described in Section 3.2.2.
- the `StandardElastoViscoPlasticity` brick, which is now described.

This `StandardElastoViscoPlasticity` brick is used to describe a specific class of strain based behaviours based on an additive split of the total strain  $\underline{\varepsilon}^{\text{to}}$  into an elastic part  $\underline{\varepsilon}^{\text{el}}$  and an one or several inelastic strains describing plastic (time-independent) flows and/or viscoplastic (time-dependent) flows:

$$\underline{\varepsilon}^{\text{to}} = \underline{\varepsilon}^{\text{el}} + \sum_{i_p=0}^{n_p} \underline{\varepsilon}_{i_p}^{\text{P}} + \sum_{i_{vp}=0}^{n_{vp}} \underline{\varepsilon}_{i_{vp}}^{\text{VP}}$$

The brick decomposes the behaviour into two components:

- The stress potential which defines the relation between the elastic strain  $\underline{\varepsilon}^{\text{el}}$  and possibly some damage variables and the stress  $\underline{\sigma}$ . As the definition of the elastic properties can be part of the definition of the stress potential, the thermal expansion coefficients can also be defined in the block corresponding to the stress potential.
- A list of inelastic flows. Inelastic flows are defined by:
  - A stress criterion. The following criteria are available: `von Mises`, `Hill 1948`, `Drucker 1949`, `Hosford 1972`, `Barlat 2004`, etc...
  - A flow criterion. By default the flow criterion is the same as the stress criterion.
  - A set of isotropic hardening rules. The following rules are available: `Linear`, `Voce` and `Swift`.
  - A set of kinematic hardening rules. The following rules are available: `Prager`, `Armstrong-Frederick`, etc...

A complete description of the features provided by the `StandardElastoViscoPlasticity` brick can be found in the dedicated web page.<sup>5</sup>

Figure 2 shows how to use this brick to implement a perfect plastic behaviour based on the Hosford criterion (see Section 2).

The brick handles many aspects of the behaviour integration. For example, if several yield surfaces are involved, a set of boolean values is introduced associated with the activation or deactivation of each yield surface: after each convergence of the implicit system, consistency of the activation/deactivation of each yield surface is checked. If one system' status changes, the Newton iterations are restarted until a state satisfying the implicit equations and the consistency checks is found.

<sup>5</sup><http://tfel.sourceforge.net/StandardElastoViscoPlasticityBrick.html>.

```

@DSL Implicit;
@Behaviour StandardElastoViscoPlasticityPlasticityTest9;
@Author Thomas Helfer;
@Date 23/04/2018;

@ModellingHypotheses {"."+};

@Epsilon 1.e-16;
@IterMax 100;
@Theta 1;

@Brick "StandardElastoViscoPlasticity" {
  stress_potential : "Hooke" {young_modulus : 160e9, poisson_ratio : 0.3},
  inelastic_flow : "Plastic" {
    criterion : "Hosford" {a : 6},
    isotropic_hardening : "Linear" {R0 : 120e6}
  }
};

```

Figure 2: Example of the `StandardElastoViscoPlasticity` brick usage.

This brick shows a deep move in `MFront`, as no more bare `C++` code is required to implement a new behaviour. The syntax used is only declarative and strongly inspired by the JSON format,<sup>6</sup> which is meant to be simple and readable. The underlying implementation has been designed so that graphical user interfaces can easily be build which would allow an even simpler usage in future versions.

However, it is important to note that the user still can add additional state variables and associated implicit equations.

## 3.2 Single crystal behaviours in `MFront`

Single crystal behaviours are an important use case of `MFront` (25–27). To simplify their implementations, a set of keywords to describe the crystal structure, slip systems and interaction matrices (Section 3.2.1), and a dedicated brick (Section 3.2.2), have been introduced.

### 3.2.1 The `TFELNUMODIS` library

Support for writting single crystal behaviours have been greatly improved thanks to the `TFELNUMODIS` library, which borrows code for the `NUMODIS` project (28).

The crystal structure can be defined using the `@CrystalStructure` keyword. The following crystal structures are supported: `Cubic` (cubic structure), `BCC` (body centered cubic structure), `FCC` (face centered cubic structure) and `HCP` (hexagonal closed-packed structures).

A single slip systems family can be defined by one of the following synonymous keywords: `@SlidingSystem`, `@GlidingSystem` or `@SlipSystem`. Several slip systems families can be defined by `@SlidingSystems`, `@GlidingSystems` or `@SlipSystems`.

Two kind of interaction matrices can be defined:

- The first interaction matrix is defined through the `@InteractionMatrix` keyword and is meant to describe the effect of dislocations on hardening.
- The second interaction matrix is defined through the `@DislocationsMeanFreePathInteractionMatrix` keyword and is meant to evaluate the effect of all the dislocations on the mean free path of dislocations of a specific system.

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<sup>6</sup>JavaScript Object Notation. See <https://en.wikipedia.org/wiki/JSON>.

Those keywords are fully documented on the dedicated page.<sup>7</sup>

### 3.2.2 Description of the FiniteStrainSingleCrystal brick

The `FiniteStrainSingleCrystal` brick is based on a thermodynamic framework which describes the (visco)-plasticity of single crystal (see (25, 29–31) for further details). A multiplicative decomposition  $\mathbf{F}_e \cdot \mathbf{F}_p$  of the deformation gradient  $\mathbf{F}$  is assumed. The driving force for plasticity is the Mandel stress tensor defined in the intermediate configuration.

The `FiniteStrainSingleCrystal` brick handles all the kinematic aspects related to the multiplicative decomposition  $\mathbf{F}_e \cdot \mathbf{F}_p$ , the definition of the Mandel stress tensor and its derivative (if required) and the computation of the consistent tangent operator.

The user can thus focus on the definition on the constitutive equations describing the plastic evolutions of each slip systems.

The hidden details of the implementation closely follows the one described in the `Code_Aster` documentation (31).

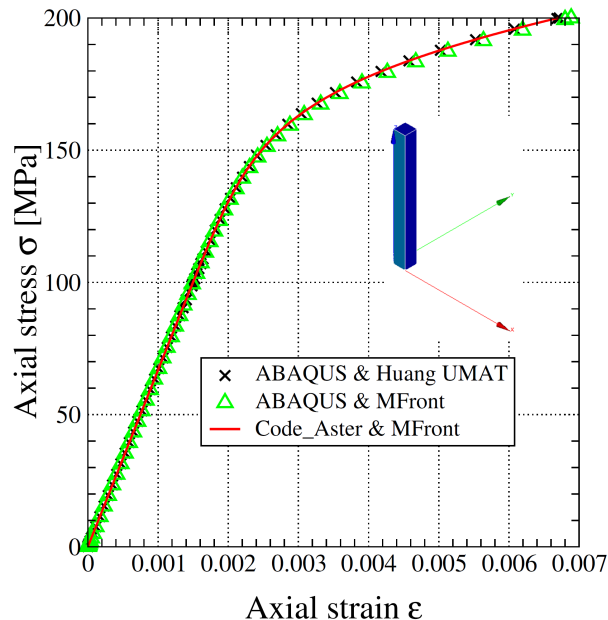


Figure 3: Benchmark of ABAQUS UMAT Fortran subroutine given by Huang (32) and MFront implementation. A single crystalline copper bar (FCC crystal structure, slip system  $\{111\} \langle 110 \rangle$ ) is subjected to a tensile load of  $200 \text{ MPa}$  in  $1 \text{ s}$ . More details of the parameters used for the test case can be found in Reference (32).

Figure 3 shows how this brick has been used to implement a phenomenological crystal plasticity model proposed by Huang (32). This figure also shows that the same implementation works equally in Abaqus/Standard and Code/Aster.

## 4 Solver interfaces

### 4.1 The generic behaviour interface

Whereas other interfaces target a specific solver and thus are restricted by choices made by this specific solver, the `generic` interface has been created for developers of homebrew solvers who are able to modify their code to take full advantage of `MFront` behaviours.

<sup>7</sup><http://tfel.sourceforge.net/singlecrystal.html>.

This interface is tightly linked with the `MFrontGenericInterfaceSupport` project which is available on [github](https://github.com).<sup>8</sup> This project has a more liberal licence than `TFEL` which allows it to be included in both commercial and open-source solvers/library. This licensing choice explains why this project is not part of the `TFEL`. While the core of the project is written in `C++`, bindings are provided for the following languages: `C`, `fortran`, `python`. The following solvers already use this project to create an interface with `MFront`: `XPer` (33), `OpenGeoSys` (34). An interface to `MoFEM` is currently being discussed (35).

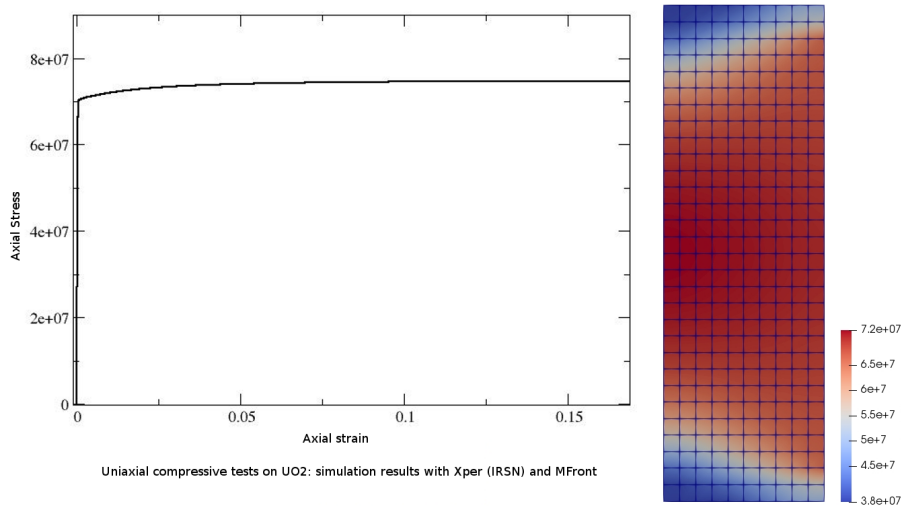


Figure 4: First results on the coupling of `MFront` and `XPer` through the `MFrontGenericInterfaceSupport` project

Figure 4 illustrates the coupling between `MFront` and `XPer` to the simulation the uniaxial compression tests on Uranium dioxyde (see (36, 37) for details about the behaviour used).

## 4.2 New interfaces

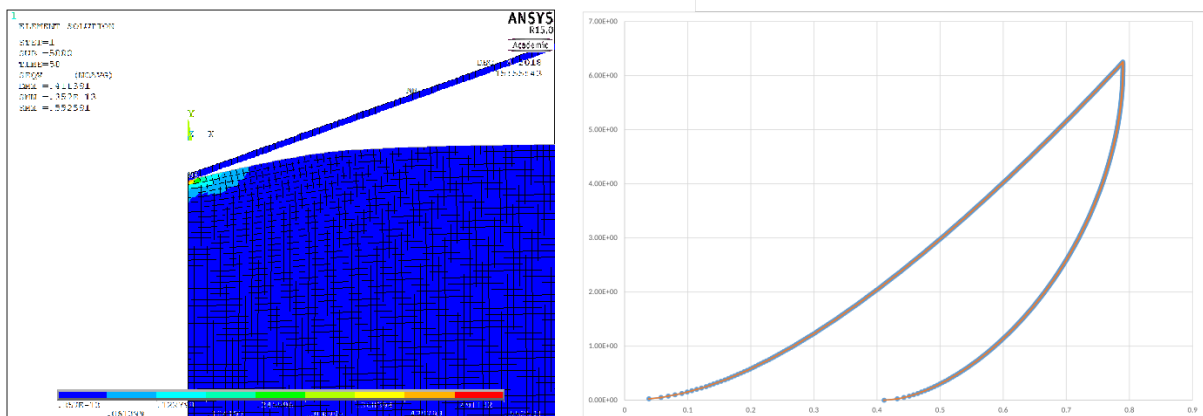


Figure 5: Qualification of the `Ansys` interface on the axisymmetrical simulation of the indentation of a viscoelastic material. Cauchy Stress value for the maximal imposed displacement (left). Comparison of the force-displacement curves obtained with a reference implementation (38) and a `MFront`' implementation: results are undistinguishable (right)

Two new interfaces are now available:

- An interface for the `Ansys` APDL solver. Figure 5 shows an example of `MFront` behaviour usage in `Ansys` (`Ansys 15` under `Windows` using the `Visual Studio 15` compiler suite).

<sup>8</sup><https://github.com/thelfer/MFrontGenericInterfaceSupport>.

- An interface to the open-source CalculiX solver (16, 17).

## 5 Numerical improvements

### 5.1 Robustness of the implicit scheme

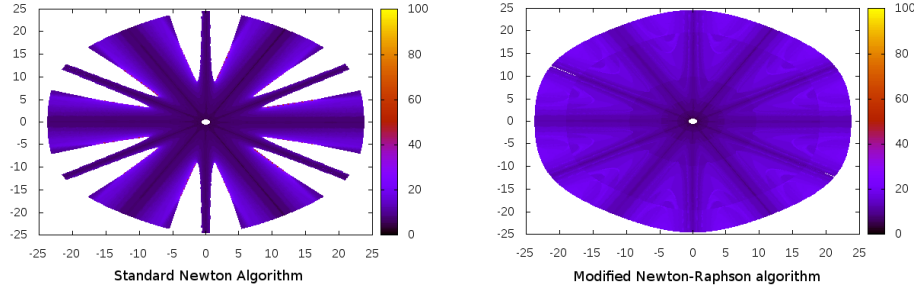


Figure 6: Comparison of the robustness of two implicit scheme algorithms for a perfect plastic behaviour based on the Hosford criterion using the test proposed by Scherzinger (21)

To illustrate some of the work made to increase the robustness of the implicit scheme, let us consider the perfect plastic behaviour based on the Hosford equivalent stress whose implementation has been described in Section 3.1.

For such a behaviour, Scherzinger proposed a test of the robustness of the integration scheme (21). For a given direction the  $\pi$  plane, a reference strain increment is chosen which would lead to an elastic prediction of the strain whose equivalent stress (using Hosford criterion) is equal to the yield stress. A set of tests is then performed by imposing, in one step, this reference strain increment amplified by an given factor. This amplification factor starts from 1 and is increased up to a value corresponding to an integration failure or a maximal value of 30 if no integration failure occurs. The number of iterations required to reach convergence is saved.

Figure 6 reports the results of this test in the case an Hosford exponent  $a$  equal to 6. Two algorithms are compared: the standard Newton-Raphson algorithm and for a slightly modified version of this algorithm. The modification consists in testing the value of the Hosford equivalent stress during the Newton iterations: if this value exceeds the yield criterion by a factor 1.5, the Newton-step amplitude is divided by a factor 2. The figure shows that this slight modification strongly increases the robustness of the algorithm. This modification has been used on the computation of the deep drawing of a cup depicted on Figure 1.

The results of this test for various values of the Hosford exponent are reported on a dedicated web page<sup>9</sup>. For very high values of  $a$ , the standard Newton-Raphson algorithm and the modified version perform poorly. One has to combine an accurate algorithm for the computation of the eigenvalues and eigen vectors (the Jacobi algorithm)<sup>10</sup> and the Levenberg-Marquardt algorithm to ensure convergence.

### 5.2 Overall work on the numerical stability

<sup>9</sup><http://tfel.sourceforge.net/hosford.net>

<sup>10</sup>By default, TFEL will use an explicit algorithm based on Cardano formulae which is faster but less accurate than the Jacobi algorithm. A comparison of the various algorithms available available in TFEL can be found in the release note of versions 3.1 available here: <http://tfel.sourceforge.net/release-notes-3.1.html>. The implementation of the Jacobi algorithm has been adapted from Joachim Kopp' work (39, 40).

Table 1: Test on  $10^6$  random symmetric tensors  $\underline{s}$  in double precision  $\Delta_\infty = \max_{\underline{s}} \max_{i \in [1,2,3]} \|\underline{s} \cdot \vec{v}_i - \lambda_i \vec{v}_i\|$ .

Algorithm	$\Delta_\infty$	Time ratio
TFELEIGENSOLVER	7.75e-14	1
FSESJACOBIEIGENSOLVER	1.05e-15	1.94
FSESQLEIGENSOLVER	3.30e-15	1.45
FSESHYBRIDEIGENSOLVER	3.53e-10	0.61
FSESANALYTICALEIGENSOLVER	1.09e-09	0.62

Authors put much emphasis on working on the overall numerical stability of the algorithms provided in the `TFEL/Math` library. To illustrate this, Table 1 compares the accuracy of various eigen solvers, comparing the default solver of `TFEL/Math` (`TFELEIGENSOLVER`), based on the Cardano formulae, to various solvers proposed by Joachim Kopp which have been introduced in `TFEL/Math` (39, 40). While the default solver provides a good compromise in terms of accuracy and efficiency, the Jacobi solver is the most accurate and seems fairly insensitive to the optimisation flags used.

This work now allows to safely use more aggressive optimisation flags which allow the compilers to ignore some of the rules imposed by the IEEE754 standard<sup>11</sup>.

## 6 Documentation: The gallery and the `MFrontGallery` project

The `MFront` gallery is meant to present well-written implementation of behaviours that will be updated to follow `MFront` latest evolutions. In each case, the integration algorithm is fully described.

The `MFrontGallery` project is a `cmake` project which builds material libraries for all the codes and/or languages supported by `MFront` based on the implementation described in the gallery. The purpose of this project is twofold:

- It delivers ready-to-use shared libraries for a wide variety of phenomena.
- It provides an example of how to build a compilation project for `MFront` files, including lots of useful `cmake` macros and recipes to build shared libraries and add tests.

The `MFrontGallery` project is available as a `github` repository<sup>12</sup>.

## 7 Conclusions

This paper has highlighted some improvements made in the versions 3.1 and 3.2 of `TFEL` and `MFront`. Mechanical behaviours can be written even more easily than in previous versions and performances are competitive with built-in behaviour implementations of most mechanical solvers.

The `MFront` users' community is steadily increasing outside the nuclear industry and the french mechanical community: its use now encompasses a wide range of materials and applications (see Figure 7 for example).

<sup>11</sup>Namely, the `-ffast-math` option with the GNU compiler `g++`.

<sup>12</sup><https://github.com/thelfer/MFrontGallery>



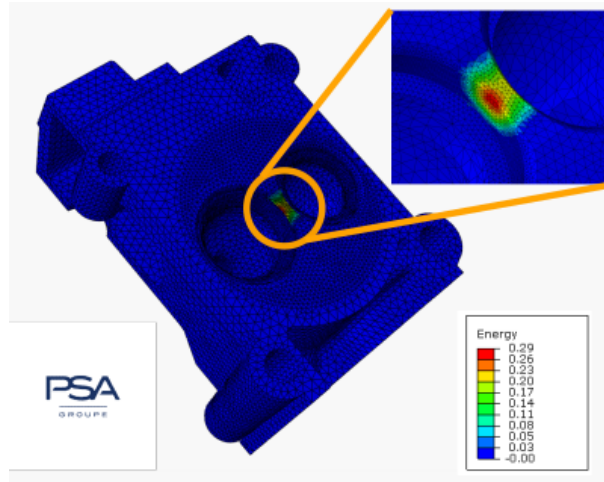


Figure 7: An example of MFront’ usage at Groupe PSA: thermo-mechanical design of an automotive single cylinder head

## 7.1 Interfaces under development

The following interfaces are under development:

- an interface for the DIANA FEA solver (41).
- an interface for the LS-DYNA solver (42).

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